

Fluids #6

p414 MC 1, 2, 7

Concept 16


p415 Problems 18, 20, ~~22~~, 46

Online - Understand Bernoulli

6

p414 - Multiple Choice

(12)

1)  Two empty soda cans, blow horizontally

• higher speed air, lower pressure

• Move closer (high P outside pushes in)

(3)

2) Roof blown off during tornado

• higher speed wind, causes lower pressure

• higher P air inside house, pushes out

3) Cut end envelope + blow air past, it bulge open

• blown air blowing past outside exerts less pressure than air inside

- Concept

1a) Partly close end hose, water squirts further why?

• Blocking opening reduces cross-sectional area $A_1 v_1 = A_2 v_2$ $\downarrow A \uparrow v$

(1)

Fill in blanks:

Blocking the opening of the hose w/ your thumb reduces the cross-sectional area. Thus by continuity eqn a smaller area means a greater horizontal speed & hence a longer travel distance

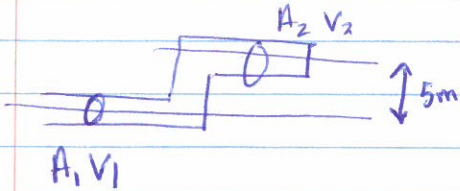
- Problems

18) $r_1 = .06 \text{ m}$
 $v_1 = 1.8 \text{ m/s}$
 $P_1 = 2.2 \times 10^5 \text{ N/m}^2$

a) $Q_1 = ? \quad Q = Av = \pi r^2 v$
 $= \pi (.060 \text{ m})^2 (1.8 \text{ m/s})$
 $= .0204 \text{ m}^3/\text{s}$

b) P_2 after go up 5m hill
 flow into $r_2 = .050 \text{ m}$

(3)



① $A_1 v_1 = A_2 v_2$

$$v_2 = \frac{A_1 v_1}{A_2} = \frac{\pi r_1^2 v_1}{\pi r_2^2}$$

$$= \frac{(.06 \text{ m})^2 (1.8 \text{ m/s})}{(.050 \text{ m})^2}$$

$$v_2 = 2.6 \text{ m/s}$$

② $P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2 = P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1$

$$P_2 = P_1 + \frac{1}{2} \rho (v_1^2 - v_2^2) - \rho g y_2$$

$$= (2.2 \times 10^5 \text{ N/m}^2) + \frac{1}{2} (1000 \text{ kg/m}^3) ((1.8 \text{ m/s})^2 - (2.6 \text{ m/s})^2)$$

$$- (1000 \text{ kg})(9.81 \text{ m/s}^2)(5.0 \text{ m})$$

$$= 1.7 \times 10^5 \text{ N/m}^2$$

(6)

20) wash skylights, 8 m above ground
 connect two hoses .8 cm to 1.0 cm
 small hose on roof, large hose faucet on ground
 Pat small was 1 atm, want $v = 6 \text{ m/s}$
 What P ground level? what speed

$$\textcircled{1} v_1 = ? \quad A_1 v_1 = A_2 v_2 \quad v_1 = \frac{A_2 v_2}{A_1} = \frac{\pi r_2^2 v_2}{\pi r_1^2}$$

$$v_1 = \frac{(.8 \text{ cm})^2 (6.0 \text{ m/s})}{(1.0 \text{ cm})^2} = 3.8 \text{ m/s}$$

↙ ground level

(2)

$$\textcircled{2} P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2 = P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1$$

$$P_1 = P_2 + \frac{1}{2} \rho (v_2^2 - v_1^2) + \rho g y_2$$

$$= 1.0 \times 10^5 \text{ N/m}^2 + \frac{1}{2} (1000 \text{ kg/m}^3) (6.0 \text{ m/s})^2 - (3.8 \text{ m/s})^2 + (1000 \text{ kg/m}^3) (9.8 \text{ m/s}^2) (8.0 \text{ m})$$

$$P_1 = 1.9 \times 10^5 \text{ N/m}^2$$

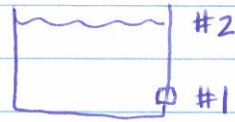
6

4(c) cooler filled w/ water has hole

$$r = .40 \text{ m}$$

$$h = 1.0 \text{ m}$$

$$A = .4 \text{ m} \times .6 \text{ m}$$



a) initial flow rate

$$P_1 = P_2 = P_{\text{atm}}$$

$$\textcircled{1} P_1 + \frac{1}{2} \rho v_1^2 + \rho g y_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

$$v_1 = \sqrt{2gy_2} = \sqrt{2(9.81 \text{ m/s}^2)(1.0 \text{ m})} = 4.4 \text{ m/s}$$

$$\textcircled{2} Q = Av_1 = \pi r^2 v_1 = \pi (.004 \text{ m})^2 (4.4 \text{ m/s})$$

$$Q_1 = 2.2 \times 10^{-4} \text{ m}^3/\text{s}$$

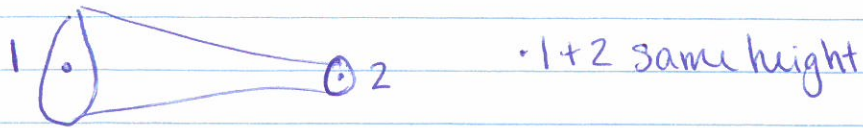
$$\text{b) } t_{\text{empty}} = ? \quad Q = \frac{\Delta V}{\Delta t} \quad t = \frac{\Delta V}{Q}$$

$$t = \frac{(.40 \text{ m}) \times (.60 \text{ m}) \times (1.0 \text{ m})}{2.2 \times 10^{-4} \text{ m}^3/\text{s}} = 1090 \text{ s}$$

c) flow rate slows w/ time so $v_1 \downarrow$, $Q \downarrow$

in reality takes more time

- Online - Understand Bernoulli



a) $A_1 > A_2$ $A_1 v_1 = A_2 v_2$ $\downarrow A$ $\uparrow v$ $\downarrow P$

$P_1 > P_2$ lower P

b) net force causes fluid to

increase v

c) If point 2 was higher point, how ΔP compare?

• P based on v change & h change

• larger P drop occurring than purely horizontal

d) physical point of view - pressure drop larger

Greater amount of work is needed to balance ...

• Increase in PE from elevation change