

HW 4 p 269 P 32

p 311 P 22, 28, 31, 60

online ① Sculpture in Equilibrium

② Axis of Rotation & I Rank

p269 - Problem

32) Two people hold hands on rollerblades

1m apart

 $m_1 = 50\text{kg}$ $m_2 = 75\text{kg}$ a) Estimate center of mass?
(from m_1)

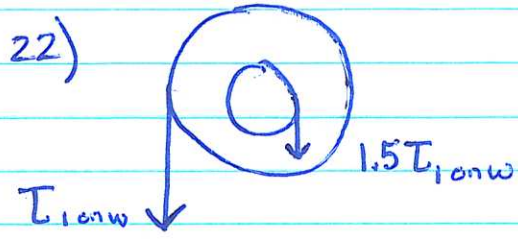
$$x_{cm} = \frac{m_1 x_1 + m_2 x_2}{m_1 + m_2} = \frac{75\text{kg}(1\text{m})}{50\text{kg} + 75\text{kg}}$$

$$x_{cm} = 0.60\text{m from } m_1$$

b) Push off + roll 4m apart. New C.M.?

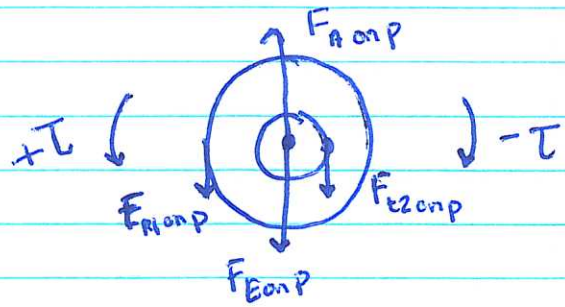
 x_{cm} stays same \rightarrow no Fnet from external

p 311 - Problems



• solid 2 part pulley
 $r_1 = 2.0a$ $r_2 = 1.5a$

a) Force diagram



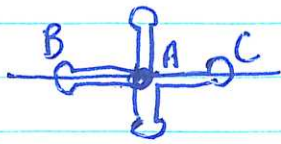
b) $\sum \tau = T_1 - T_2 = F_1 r_1 - F_2 r_2$
 $= T_1 (2a) - 1.5T_1 (1.5a)$
 $= 2T_1 a - 2.25T_1 a$
 $= -.25T_1 a$

c) sign ω ? Initially +, will become -

d) sign α ? Negative, will not change

(4)

28)



$I = ?$

- massless rods
- axis \perp to paper through point A

$$I = \sum mr^2 = 4(m)(1.0\text{m})^2 = 4m$$

31)

$$\begin{aligned} \omega_0 &= 0 \text{ rad/s} \\ \omega_f &= 1.5 \text{ rad/s} \\ t &= 8.0 \text{ s} \end{aligned}$$

merry go round mechanic
(solid disk)

$\tau = ?$

$$\begin{aligned} r &= 5.0 \text{ m} \\ m &= 25000 \text{ kg} \end{aligned}$$

$$\textcircled{1} \alpha = \frac{\Delta\omega}{t} = \frac{1.5 \text{ rad/s}}{8 \text{ s}} = 0.19 \text{ rad/s}^2$$

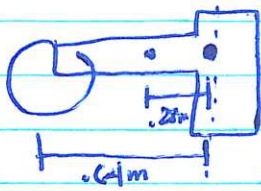
$$\textcircled{2} \tau = I\alpha = \frac{1}{2} m R^2 \alpha$$

$$= \frac{1}{2} (25000 \text{ kg})(5 \text{ m})^2 (0.19 \text{ rad/s}^2)$$

$$= 5.9 \times 10^4 \text{ Nm}$$

4

66) Bowling ball throw



$$l = .64\text{m}$$

$$\alpha = ?$$

$$m_b = 2.7\text{kg}$$

$$I_{\text{arm}} = .48\text{kgm}^2$$

$$\alpha = \frac{\sum \tau}{I}$$

$$M_{\text{arm}} = 3.5\text{kg}$$

$$r_{\text{cm}} = .28\text{m}$$

$$\textcircled{1} \sum \tau = \tau_{\text{ball}} + \tau_{\text{arm}}$$

$$= m_b g r_{\text{ball}} + M_{\text{arm}} g r_{\text{arm}}$$

$$= (2.7\text{kg})(9.81\text{m/s}^2)(.64\text{m}) + (3.5\text{kg})(9.81\text{m/s}^2)(.28\text{m})$$

$$= 26.6\text{Nm}$$

$$\textcircled{2} I_{\text{net}} = I_{\text{ball}} + I_{\text{arm}}$$

$$= m r^2 + I_{\text{arm}}$$

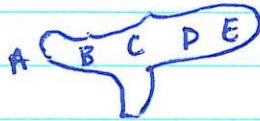
$$= (2.7\text{kg})(.64\text{m})^2 + .48\text{kgm}^2$$

$$= 1.59\text{kgm}^2$$

$$\textcircled{3} \alpha = \frac{\sum \tau}{I_{\text{net}}} = \frac{26.6\text{Nm}}{1.59\text{kgm}^2} = 16.7\text{rad/s}^2$$

- Online

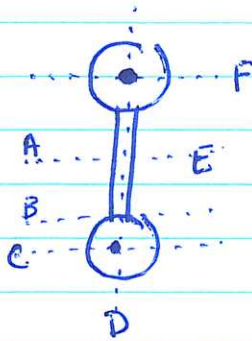
① Sculpture in Equilibrium



Where is center of mass?

C - right above support

② Axis of Rotation & I Rank



• Two identical uniform solid spheres attached by solid thin rod

• The rod lies on line connecting center of mass of 2 spheres

- ABCD plane of the page
- EF ⊥ to plane

Rank I about the axes indicated (large to sm)

C	B	A	D
F		E	

$$\left(\begin{array}{ll} A: mr^2 + mr^2 = 2mr^2 & E \text{ same as } A \\ C: m(2r)^2 = 4mr^2 & F \text{ same as } C \end{array} \right)$$